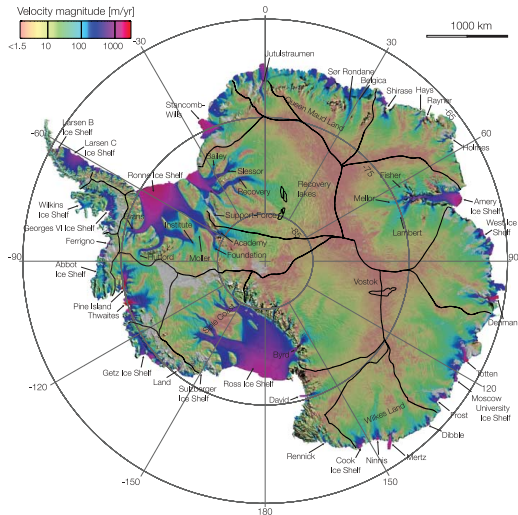


# The Role of Granular Mechanics and Porous Flow for Ice Sheet Behavior in a Changing Climate

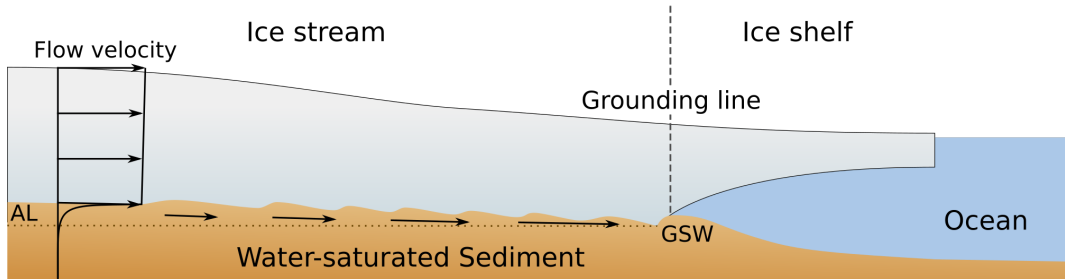
Anders Damsgaard, Jenny Suckale, Liran Goren

<https://adamsgaard.dk>  
<gopher://adamsgaard.dk>  
[anders@adamsgaard.dk](mailto:anders@adamsgaard.dk)

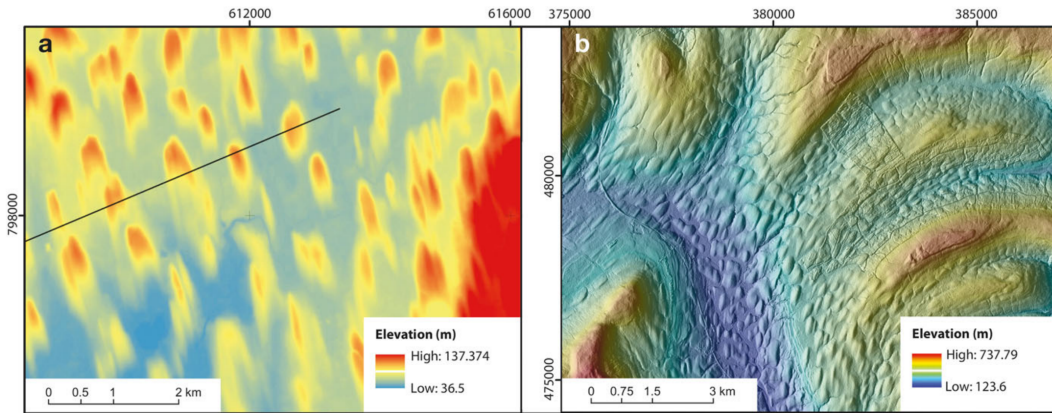
**ESCO 2020:** Climate MS, 2020-06-08



## Subglacial sediment transport

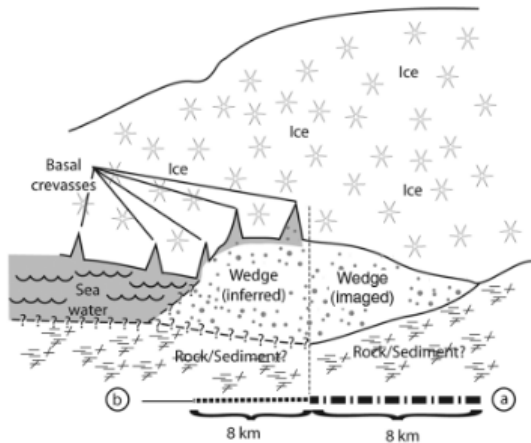


## Subglacial sediment transport

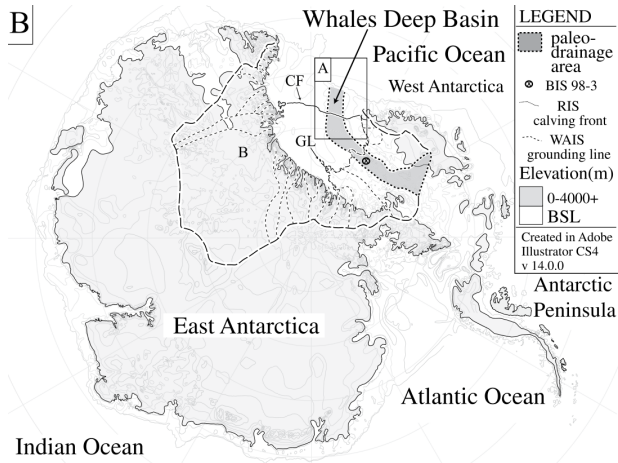




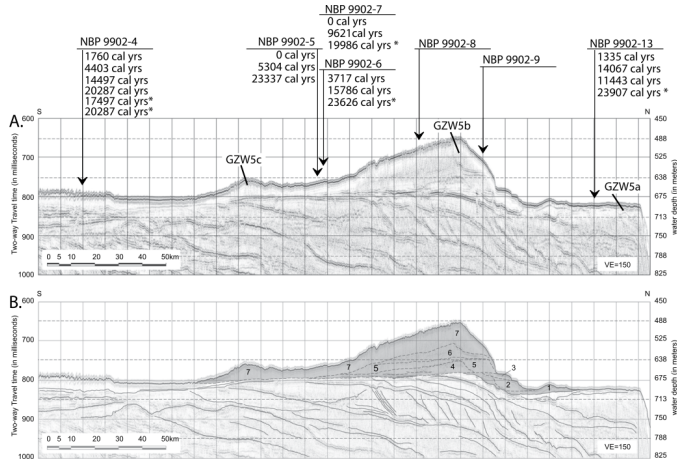
## Grounding-zone wedges



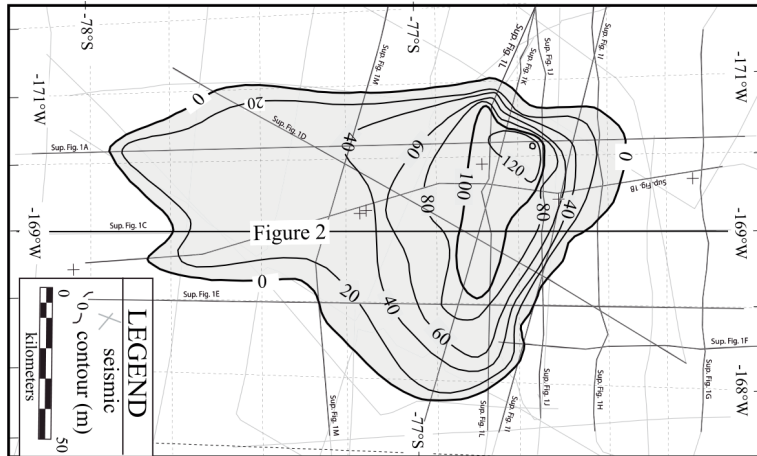
## Palaeo-grounding zone wedges



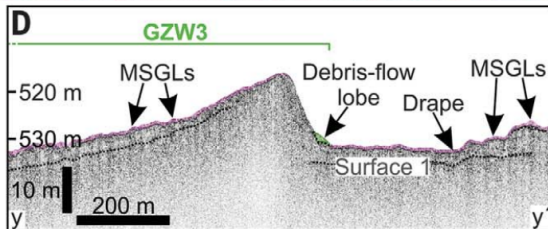
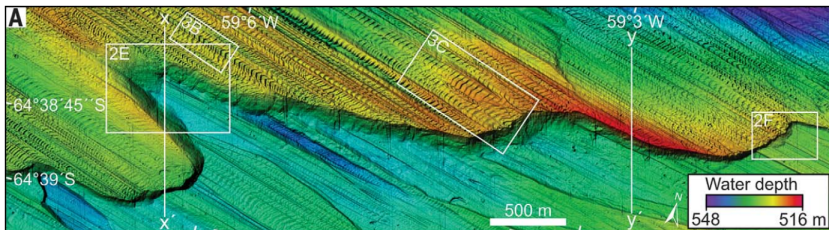
## Palaeo-grounding zone wedges



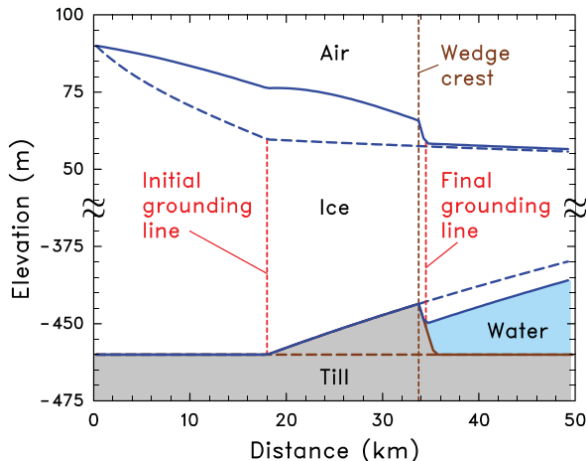
## Palaeo-grounding zone wedges



## Palaeo-grounding zone wedges



## Ice-stream stabilization





No model for till transport



No physically-based modeling



Introduction  
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Granular rheology  
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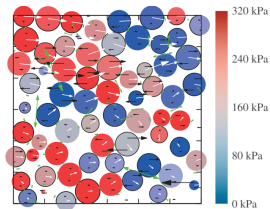
Validation  
○○○○

Water-sediment simulations  
○○○○○○○

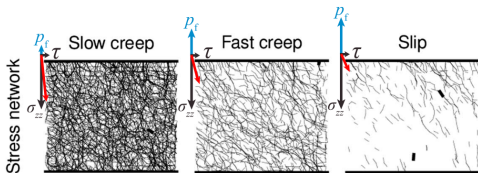
Conclusions  
○○

# Granular modeling

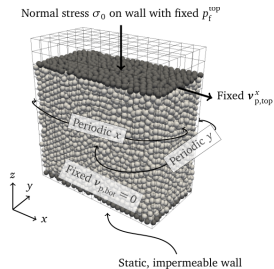
# Particle-scale modeling: Discrete-element method



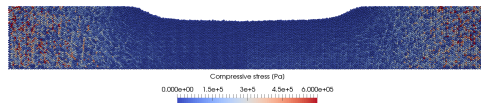
Damsgaard et al. 2013 *J. Geophys. Res.*



Damsgaard et al. 2016 *Geophys. Res. Lett.*



Damsgaard et al. 2015 *The Cryosphere*

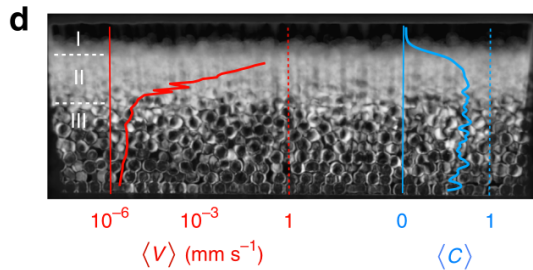
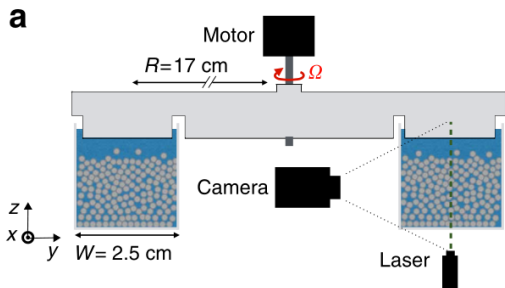


Damsgaard et al. 2017 *J. Glaciol.*



# Continuum modeling of granular mechanics

# Phase transitions in granular materials





## Local rheology for dense granular flows: $\mu(I)$ , $\Phi(I)$

$$I = \frac{\dot{\gamma}d}{\sqrt{N/\rho}}$$

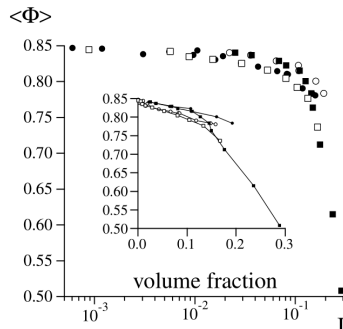
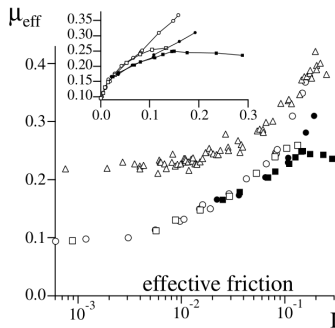
Jop et al. 2005 *J. Fluid Mech.*:

$$\tau = \mu(I)N$$

$$\mu(I) = \mu_s + \frac{\mu_2 - \mu_s}{I_0/I + 1}$$

Pouliquen et al. 2006 *J. Stat. Mech.*:

$$\Phi(I) = \Phi_{\max} - (\Phi_{\max} - \Phi_{\min})I$$



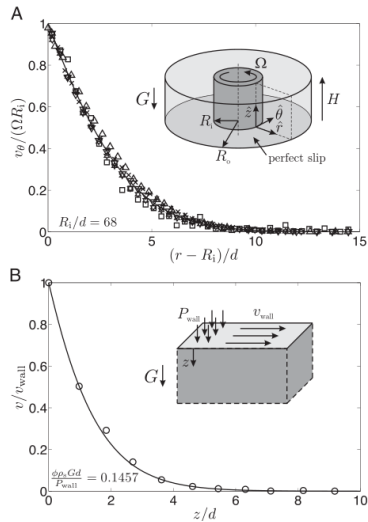
# Non-local granular fluidity rheology

$$\dot{\gamma} = g(\mu, N)\mu$$

$$g_{\text{local}}(\mu, N) = \begin{cases} \sqrt{d^2 N / \rho_s (\mu - \mu_s)} / (b\mu) & \text{if } \mu > \mu_s \\ 0 & \text{if } \mu \leq \mu_s \end{cases}$$

$$\nabla^2 g = \frac{1}{\xi^2(\mu)} (g - g_{\text{local}})$$

$$\xi(\mu) = \frac{Ad}{\sqrt{|\mu - \mu_s|}}$$



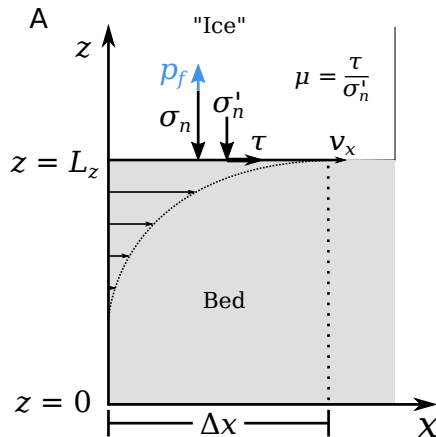


## CNGF-PF: Cohesive NGF w. pore fluid

$$\frac{\partial p_f}{\partial t} = \frac{1}{\underbrace{\phi \mu_f \beta_f}_{\text{Spatial diffusion}}} \nabla \cdot (k \nabla p_f)$$

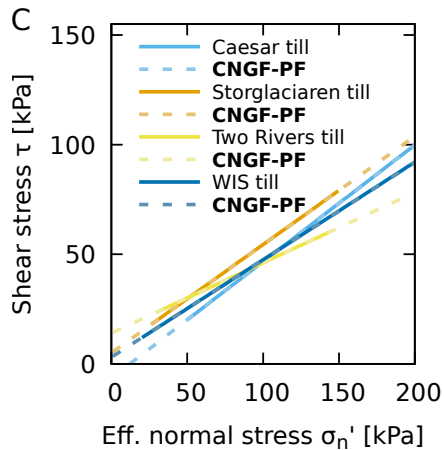
$$\sigma'_n = \sigma_n - p_f$$

## Model setup



# Validation

## Mohr Coulomb





## Granular modeling: Discrete-element method vs. continuum model

### sphere

`git://adamsgaard.dk/sphere`

C++, Nvidia C, cmake, Python, Paraview

massively parallel, GPGPU

detailed physics and fluid-grain coupling

20,191 LOC

3 months on nvidia tesla k40

### 1d-fd-simple-shear

`git://adamsgaard.dk/1d_fd_simple_shear`

C99, makefiles, gnuplot

single threaded

simple physics, simple fluid-grain coupling

2,348 LOC

70 ms on 2012 laptop

Introduction  
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○○○○○○○○

Granular rheology  
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○○○

Validation  
○○○○

**Water-sediment simulations**  
●○○○○○○

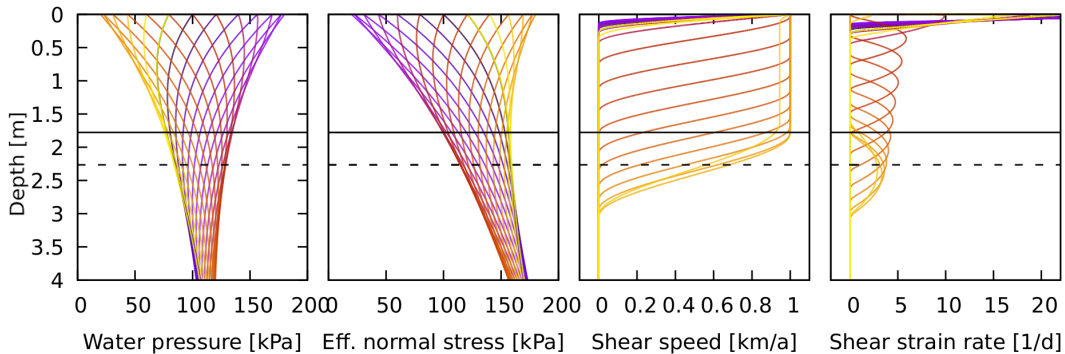
Conclusions  
○○

# Water-sediment simulations





## Water-sediment simulations

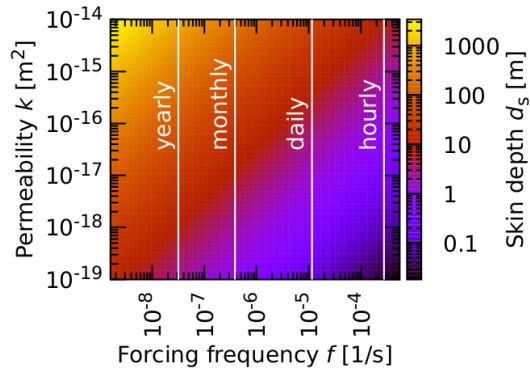


## Deep or shallow deformation?

$$d_s = \sqrt{\frac{k}{\phi \eta_f \beta_f \pi f}}$$

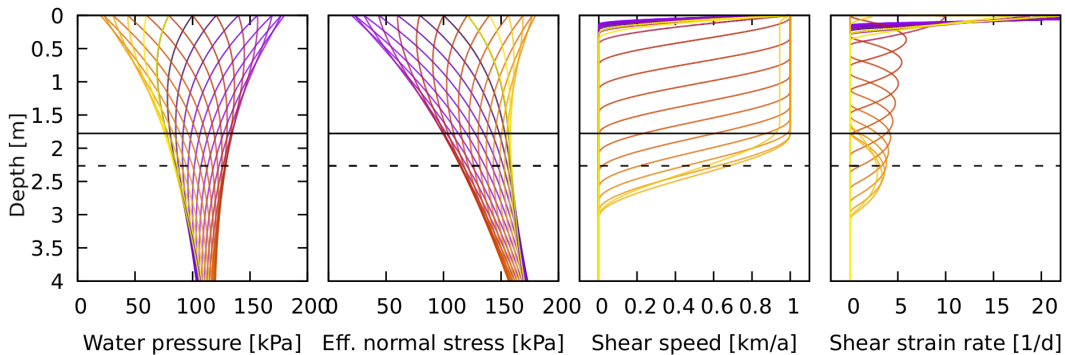
## Deep or shallow deformation?

$$d_s = \sqrt{\frac{k}{\phi \eta_f \beta_f \pi f}}$$

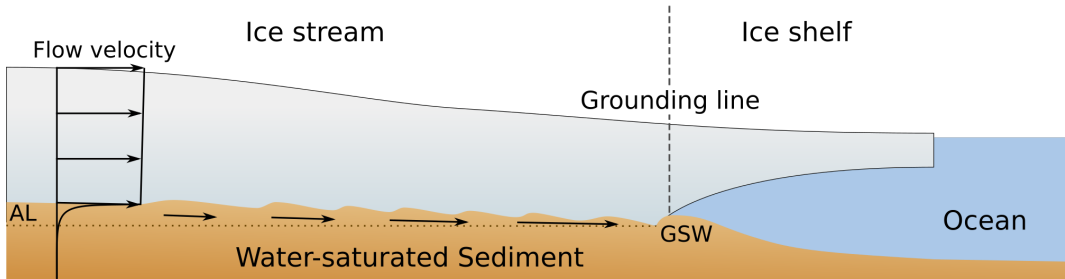




## Water-sediment simulations



## Next steps: Ice-water-sediment coupling



## Conclusions

- First-principles granular rheologies promising for coupled simulations
- Rheology consistent with critical-state sediment mechanics and laboratory experiments
- Computationally lightweight compared to particle-based methods
- Towards testable field predictions of subglacial deformation and glacier dynamics

## Resources

### Slides:

<https://adamsgaard.dk/npub/esco2020-damsgaard.pdf>

### Source code:

[https://src.adamsgaard.dk/1d\\_fd\\_simple\\_shear](https://src.adamsgaard.dk/1d_fd_simple_shear)

### Preprint: “Evolving basal slip under glaciers and ice streams”

<https://arxiv.org/abs/2002.02436>